

# Reasoning with Probabilistic Logic Programming Languages

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# Outline

- Exact inference
- Approximate inference
- Parameter learning
- Structure learning



## Inference for PLP under DS

- EVID: compute an unconditional probability  $P(e)$ , the probability of evidence (also query in this case).
- COND: compute the conditional probability distribution of the query given the evidence, i.e. compute  $P(q|e)$
- MPE or *most probable explanation*: find the most likely value of all non-evidence atoms given the evidence, i.e. solving the optimization problem  $\arg \max_q P(q|e)$
- MAP or *maximum a posteriori*: find the most likely value of a set of non-evidence atoms given the evidence, i.e. finding  $\arg \max_q P(q|e)$ . MPE is a special case of MAP where  $Q \cup E = H_T$ .
- DISTR: compute the probability distribution or density of the non-ground arguments of a conjunction of literals  $q$ , e.g., computing the probability density of  $X$  in goal  $mix(X)$  of the Gaussian mixture



# Weight Learning

- Given
  - model: a probabilistic logic model with unknown parameters
  - data: a set of interpretations
- Find the values of the parameters that maximize the probability of the data given the model
- Discriminative learning: maximize the conditional probability of a set of outputs (e.g. ground instances for a predicate) given a set of inputs
- Alternatively, the data are queries for which we know the probability: minimize the error in the probability of the queries that is returned by the model



# Structure Learning

- Given
  - language bias: a specification of the search space
  - data: a set of interpretations
- Find the formulas and the parameters that maximize the likelihood of the data given the model
- Discriminative learning: again maximize the conditional likelihood of a set of outputs given a set of inputs



# Inference for PLP under DS

- Computing the probability of a query (no evidence)
- Knowledge compilation:
  - compile the program to an intermediate representation
    - Binary Decision Diagrams (BDD) (ProbLog [De Raedt et al. IJCAI07], `cplint` [Riguzzi AIIA07,Riguzzi LJIGPL09], PITA [Riguzzi & Swift ICLP10])
    - deterministic, Decomposable Negation Normal Form circuit (d-DNNF) (ProbLog2 [Fierens et al. TPLP15])
    - Sentential Decision Diagrams
  - compute the probability by weighted model counting



# Inference for PLP under DS

- Bayesian Network based:
  - Convert to BN
  - Use BN inference algorithms (CVE [Meert et al. ILP09])
- Lifted inference



# Knowledge Compilation

- Assign Boolean random variables to the probabilistic rules
- Given a query  $Q$ , compute its **explanations**, assignments to the random variables that are sufficient for entailing the query
- Let  $K$  be the set of all possible explanations
- Build a Boolean formula  $F(Q)$
- Build a BDD representing  $F(Q)$





$sneezing(X) \leftarrow flu(X), flu\_sneezing(X).$   
 $sneezing(X) \leftarrow hay\_fever(X), hay\_fever\_sneezing(X).$   
 $flu(bob).$   
 $hay\_fever(bob).$   
 $0.7 :: flu\_sneezing(X).$   
 $0.8 :: hay\_fever\_sneezing(X).$

# Definitions

- **Composite choice**  $\kappa$ : consistent set of atomic choices  $(C_i, \theta_j, l)$  with  $l \in \{1, 2\}$
- Set of worlds compatible with  $\kappa$ :  $\omega_\kappa = \{w_\sigma \mid \kappa \subseteq \sigma\}$
- **Explanation**  $\kappa$  for a query  $Q$ :  $Q$  is true in every world of  $\omega_\kappa$
- A set of composite choices  $K$  is **covering** with respect to  $Q$ : every world  $w$  in which  $Q$  is true is such that  $w \in \omega_K$  where
$$\omega_K = \bigcup_{\kappa \in K} \omega_\kappa$$
- Example:

$$K_1 = \{ \{ (C_1, \{X/bob\}, 1) \}, \{ (C_2, \{X/bob\}, 1) \} \} \quad (1)$$

is covering for *sneezing(bob)*.



# Finding Explanations

- All explanations for the query are collected
- ProbLog: source to source transformation for facts, use of dynamic database
- `cplint` (PITA): source to source transformation, addition of an argument to predicates



# Explanation Based Inference Algorithm

- $K$  = set of explanations found for  $Q$ , the probability of  $Q$  is given by the probability of the formula

$$f_K(\mathbf{X}) = \bigvee_{\kappa \in K} \bigwedge_{(C_i, \theta_j, l) \in \kappa} (X_{C_i \theta_j} = l)$$

where  $X_{C_i \theta_j}$  is a random variable whose domain is 1, 2 and  $P(X_{C_i \theta_j} = l) = P_0(C_i, l)$

- Binary domain: we use a Boolean variable  $X_{ij}$  to represent  $(X_{C_i \theta_j} = 1)$
- $\overline{X_{ij}}$  represents  $(X_{C_i \theta_j} = 2)$



## Example

A set of covering explanations for *sneezing(bob)* is  $K = \{\kappa_1, \kappa_2\}$

$$\kappa_1 = \{(C_1, \{X/bob\}, 1)\} \quad \kappa_2 = \{(C_2, \{X/bob\}, 1)\}$$

$$K = \{\kappa_1, \kappa_2\}$$

$$f_K(\mathbf{X}) = (X_{C_1\{X/bob\}} = 1) \vee (X_{C_2\{X/bob\}} = 1).$$

$$X_{11} = (X_{C_1\{X/bob\}} = 1) \quad X_{21} = (X_{C_2\{X/bob\}} = 1)$$

$$f_K(\mathbf{X}) = X_{11} \vee X_{21}.$$

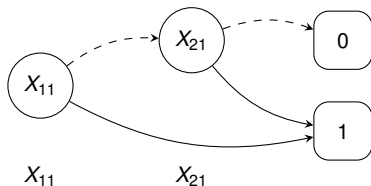
$$P(f_K(\mathbf{X})) = P(X_{11} \vee X_{21}) = P(X_{11}) + P(X_{21}) - P(X_{11})P(X_{21})$$

- In order to compute the probability, we must make the explanations mutually exclusive
- [De Raedt at. IJCAI07]: Binary Decision Diagram (BDD)



# Binary Decision Diagrams

- A BDD for a function of Boolean variables is a rooted graph that has one level for each Boolean variable
- A node  $n$  in a BDD has two children: one corresponding to the 1 value of the variable associated with  $n$  and one corresponding to the 0 value of the variable
- The leaves store either 0 or 1.

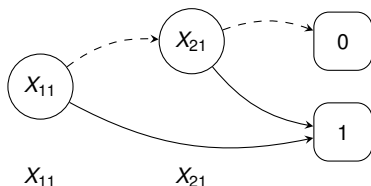


# Binary Decision Diagrams

- BDDs can be built by combining simpler BDDs using Boolean operators
- While building BDDs, simplification operations can be applied that delete or merge nodes
- Merging is performed when the diagram contains two identical sub-diagrams
- Deletion is performed when both arcs from a node point to the same node
- A reduced BDD often has a much smaller number of nodes with respect to the original BDD



# Binary Decision Diagrams



$$f_K(\mathbf{X}) = X_{11} \times f_K^{X_{11}}(\mathbf{X}) + \overline{X_{11}} \times f_K^{\overline{X_{11}}}(\mathbf{X})$$

$$P(f_K(\mathbf{X})) = P(X_{11})P(f_K^{X_{11}}(\mathbf{X})) + (1 - P(X_{11}))P(f_K^{\overline{X_{11}}}(\mathbf{X}))$$

$$P(f_K(\mathbf{X})) = 0.7 \cdot P(f_K^{X_{11}}(\mathbf{X})) + 0.3 \cdot P(f_K^{\overline{X_{11}}}(\mathbf{X}))$$





# Probability from a BDD

- Dynamic programming algorithm [De Raedt et al IJCAI07]
- Initialize map  $p$ ; Call  $\text{Prob}(\text{root})$
- Function  $\text{Prob}(n)$
- if  $p(n)$  exists, return  $p(n)$
- if  $n$  is a terminal node
  - return  $\text{value}(n)$
- else
  - $\text{prob} := \text{Prob}(\text{child}_1(n)) \times p(v(n)) + \text{Prob}(\text{child}_0(n)) \times (1 - p(v(n)))$
  - Add  $(n, \text{prob})$  to  $p$ ; return  $\text{prob}$



# Logic Programs with Annotated Disjunctions

$C_1 = \text{strong\_sneezing}(X) : 0.3 \vee \text{moderate\_sneezing}(X) : 0.5 \leftarrow \text{flu}(X).$   
 $C_2 = \text{strong\_sneezing}(X) : 0.2 \vee \text{moderate\_sneezing}(X) : 0.6 \leftarrow \text{hay\_fever}(X).$   
 $C_3 = \text{flu}(\text{bob}).$   
 $C_4 = \text{hay\_fever}(\text{bob}).$

- Distributions over the head of rules
- More than two head atoms



## Example

A set of covering explanations for *strong\_sneezing(bob)* is

$$K = \{\kappa_1, \kappa_2\}$$

$$\kappa_1 = \{(C_1, \{X/bob\}, 1)\}$$

$$\kappa_2 = \{(C_2, \{X/bob\}, 1)\}$$

$$X_{11} = X_{C_1\{X/bob\}}$$

$$X_{21} = X_{C_2\{X/bob\}}$$

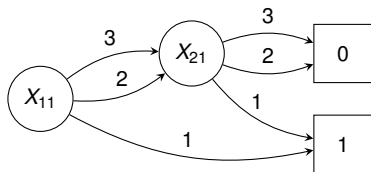
$$f_K(\mathbf{X}) = (X_{11} = 1) \vee (X_{21} = 1).$$

$$P(f_X) = P(X_{11} = 1) + P(X_{21} = 1) - P(X_{11} = 1)P(X_{21} = 1)$$

- To make the explanations mutually exclusive: Multivalued Decision Diagram (MDD)



# Multivalued Decision Diagrams



$$f_K(\mathbf{X}) = \bigvee_{l \in |X_{11}|} (X_{11} = l) \wedge f_K^{X_{11}=l}(\mathbf{X})$$

$$P(f_K(\mathbf{X})) = \sum_{l \in |X_{11}|} P(X_{11} = l) P(f_K^{X_{11}=l}(\mathbf{X}))$$

$$f_K(\mathbf{X}) = (X_{11} = 1) \wedge f_K^{X_{11}=1}(\mathbf{X}) + (X_{11} = 2) \wedge f_K^{X_{11}=2}(\mathbf{X}) + (X_{11} = 3) \wedge f_K^{X_{11}=3}(\mathbf{X})$$

$$f_K(\mathbf{X}) = 0.3 \cdot P(f_K^{X_{11}=1}(\mathbf{X})) + 0.5 \cdot P(f_K^{X_{11}=2}(\mathbf{X})) + 0.2 \cdot P(f_K^{X_{11}=3}(\mathbf{X}))$$



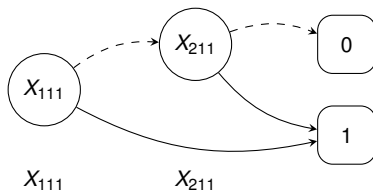
# Manipulating Multivalued Decision Diagrams

- Use an MDD package
- Convert to BDD, use a BDD package: BDD packages more developed, more efficient
- Conversion to BDD
  - Log encoding
  - Binary splits: more efficient



# Transformation to a Binary Decision Diagram

- For a variable  $X_{ij}$  having  $n$  values, we use  $n - 1$  Boolean variables  $X_{ij1}, \dots, X_{ijn-1}$
- $X_{ij} = l$  for  $l = 1, \dots, n - 1$ :  $\overline{X_{ij1}} \wedge \overline{X_{ij2}} \wedge \dots \wedge \overline{X_{ijl-1}} \wedge X_{ijl}$ ,
- $X_{ij} = n$ :  $\overline{X_{ij1}} \wedge \overline{X_{ij2}} \wedge \dots \wedge \overline{X_{ijn-1}}$ .
- Parameters:  $P(X_{ij1}) = P(X_{ij} = 1) \dots P(X_{ijl}) = \frac{P(X_{ij}=l)}{\prod_{m=1}^{l-1} (1 - P(X_{ijm}))}$ .



# Approximate Inference

- Inference problem is #P hard
- For large models inference is intractable
- Approximate inference
  - Monte Carlo: draw samples of the truth value of the query
  - Iterative deepening: gives a lower and an upper bound
  - Compute only the best  $k$  explanations: branch and bound, gives a lower bound



# Monte Carlo

- The disjunctive clause

$$C_r = H_1 : \alpha_1 \vee \dots \vee H_n : \alpha_n \leftarrow L_1, \dots, L_m.$$

is transformed into the set of clauses  $MC(C_r)$

$$MC(C_r, 1) = H_1 \leftarrow L_1, \dots, L_m, \text{sample\_head}(n, r, VC, NH), NH = 1.$$

...

$$MC(C_r, n) = H_n \leftarrow L_1, \dots, L_m, \text{sample\_head}(n, r, VC, NH), NH = n.$$

- Sample truth value of query  $Q$ :

...

```
(call(Q) -> NT1 is NT+1 ; NT1 =NT),
```

...





# Inference in DISPONTE

- The probability of a query  $Q$  can be computed according to the distribution semantics by first finding the explanations for  $Q$  in the knowledge base
- **Explanation**: subset of axioms of the KB that is sufficient for entailing  $Q$
- All the explanations for  $Q$  must be found, corresponding to all ways of proving  $Q$



# Inference in DISPONTE

- Probability of  $Q \rightarrow$  probability of the DNF formula

$$F(Q) = \bigvee_{e \in E_Q} \left( \bigwedge_{F_i \in e} X_i \right)$$

where  $E_Q$  is the set of explanations and  $X_i$  is a Boolean random variable associated to axiom  $F_i$

- Binary Decision Diagrams for efficiently computing the probability of the DNF formula



## Example

$E_1 = 0.4 :: \text{fluffy} : \text{Cat}$

$E_2 = 0.3 :: \text{tom} : \text{Cat}$

$E_3 = 0.6 :: \text{Cat} \sqsubseteq \text{Pet}$

$\exists \text{hasAnimal.Pet} \sqsubseteq \text{NatureLover}$

$(\text{kevin}, \text{fluffy}) : \text{hasAnimal}$

$(\text{kevin}, \text{tom}) : \text{hasAnimal}$



- $Q = \text{kevin} : \text{NatureLover}$  has two explanations:

$\{ (E_1), (E_3) \}$

$\{ (E_2), (E_3) \}$

- $P(Q) = 0.4 \times 0.6 \times (1 - 0.3) + 0.3 \times 0.6 = 0.348$



# BUNDLE

- Binary decision diagrams for Uncertain reasoning on Description Logic theories [Riguzzi et al. SWJ15]
- **BUNDLE performs inference over DISPONTE knowledge bases.**
- It exploits an underlying ontology reasoner able to return all explanations for a query, such as **Pellet** [Sirin et al, WS 2007]
- Then DNF formula built and converted to BDDs for computing the probability



- Tableau Reasoner for description Logics in proLog
- TRILL implements the tableau algorithm using Prolog
- It resolves the axiom pinpointing problem in which we are interested in the set of explanations that entail a query
- It returns the set of the explanations
- It can build BDDs encoding the set of explanations and return the probability



- Available online at `http://trill-sw.eu/`
- Pets example  
`http://trill-sw.eu/example/trill/peoplePets.pl`



# Parameter Learning

- Problem: given a set of interpretations, a program, find the parameters maximizing the likelihood of the interpretations (or of instances of a target predicate)
- The interpretations record the truth value of ground atoms, not of the choice variables
- Unseen data: relative frequency can't be used



# Parameter Learning

- An Expectation-Maximization algorithm must be used:
  - Expectation step: the distribution of the unseen variables in each instance is computed given the observed data
  - Maximization step: new parameters are computed from the distributions using relative frequency
  - End when likelihood does not improve anymore





# Parameter Learning

- [Thon et al. ECML 2008] proposed an adaptation of EM for CPT-L, a simplified version of LPADs
- The algorithm computes the counts efficiently by repeatedly traversing the BDDs representing the explanations
- [Ishihata et al. ILP 2008] independently proposed a similar algorithm
- LFI-PROBLOG [Gutamn et al. ECML 2011]: EM for ProbLog
- EMBLEM [Riguzzi & Bellodi IDA 2013] adapts [Ishihata et al. ILP 2008] to LPADs



# EMBLEM

- EM over Bdds for probabilistic Logic programs Efficient Mining
- Input: an LPAD; logical interpretations (data); *target* predicate(s)
- All ground atoms in the interpretations for the target predicate(s) correspond to as many queries
- BDDs encode the explanations for each query  $Q$
- Expectations computed with two passes over the BDDs



- Em over bDds for description loGics paramEter learning
- EDGE is inspired to EMBLEM [Bellodi and Riguzzi, IDA 2013]
- Takes as input a DL theory and a number of examples that represent queries.
- The queries are concept assertions and are divided into:
  - 1 positive examples;
  - 2 negative examples.
- EDGE computes the explanations of each example using BUNDLE, that builds the corresponding BDD.
  - For negative examples, EDGE computes the explanations of the query, builds the BDD and then negates it.



# Structure Learning for LPADs

- Given a trivial LPAD or an empty one, a set of interpretations (data)
- *Find the model and the parameters* that maximize the probability of the data (log-likelihood)
- SLIPCOVER: Structure Learning of Probabilistic logic program by searching OVER the clause space EMBLEM [Riguzzi & Bellodi TPLP 2015]
  - 1 Beam search in the space of clauses to find the promising ones
  - 2 Greedy search in the space of probabilistic programs guided by the LL of the data.
- *Parameter learning* by means of EMBLEM



# SLIPCOVER

- Cycle on the set of predicates that can appear in the head of clauses, either target or background
- For each predicate, beam search in the space of clauses
- The initial set of beams is generated by building a set of *bottom clauses* as in Progol [Muggleton NGC 1995]



# Mode Declarations

- Syntax

```
modeh (RecallNumber, PredicateMode) .
```

```
modeb (RecallNumber, PredicateMode) .
```

- `RecallNumber` can be a number or `*`. Usually `*`. Maximum number of answers to queries to include in the bottom clause
- `PredicateMode`: template of the form:

```
p (ModeType, ModeType, ...)
```



# Mode Declarations

- `ModeType` can be:
  - Simple:
    - $+T$  input variables of type  $T$ ;
    - $-T$  output variables of type  $T$ ; or
    - $\#T, -\#T$  constants of type  $T$ .
  - Structured: of the form  $f(\dots)$  where  $f$  is a function symbol and every argument can be either simple or structured.



# Mode Declarations

- Some examples:

```
modeb (1, mem (+number, +list)) .  
modeb (1, dec (+integer, -integer)) .  
modeb (1, mult (+integer, +integer, -integer)) .  
modeb (1, plus (+integer, +integer, -integer)) .  
modeb (1, (+integer) = (#integer)) .  
modeb (*, has_car (+train, -car))  
modeb (1, mem (+number, [+number | +list])) .
```





## Bottom Clause $\perp$

- Most specific clause covering an example  $e$
- Form:  $e \leftarrow B$
- $B$ : set of ground literals that are true regarding the example  $e$
- $B$  obtained by considering the constants in  $e$  and querying the predicates of the background for true atoms regarding these constants
- A map from types to lists of constants is kept, it is enlarged with constants in the answers to the queries and the procedure is iterated a user-defined number of times
- Values for output arguments are used as input arguments for other predicates



## Bottom Clause $\perp$

- Initialize to empty a map  $m$  from types to lists of values
- Pick a  $modeh(r, s)$ , an example  $e$  matching  $s$ , add to  $m(T)$  the values of  $+T$  arguments in  $e$
- For  $i = 1$  to  $d$ 
  - For each  $modeb(r, s)$



## Bottom Clause $\perp$

- For each possible way of building a query  $q$  from  $s$  by replacing  $+T$  and  $\#T$  arguments with constants from  $m(T)$  and all other arguments with variables
  - Find all possible answers for  $q$  and put them in a list  $L$
  - $L' := r$  elements sampled from  $L$
  - For each  $l \in L'$ , add the values in  $l$  corresponding to  $-T$  or  $-\#T$  to  $m(T)$



## Bottom Clause $\perp$

- Example:

$e = \text{father}(\text{john}, \text{mary})$

$B = \{\text{parent}(\text{john}, \text{mary}), \text{parent}(\text{david}, \text{steve}),$   
 $\text{parent}(\text{kathy}, \text{mary}), \text{female}(\text{kathy}), \text{male}(\text{john}), \text{male}(\text{david})\}$

$\text{modeh}(\text{father}(+ \text{person}, + \text{person}))$ .

$\text{modeb}(\text{parent}(+ \text{person}, - \text{person}))$ .

$\text{modeb}(\text{parent}(- \# \text{person}, + \text{person}))$ .

$\text{modeb}(\text{male}(+ \text{person}))$ .  $\text{modeb}(\text{female}(\# \text{person}))$ .

$e \leftarrow B = \text{father}(\text{john}, \text{mary}) \leftarrow \text{parent}(\text{john}, \text{mary}), \text{male}(\text{john}),$   
 $\text{parent}(\text{kathy}, \text{mary}), \text{female}(\text{kathy})$ .



## Bottom Clause $\perp$

- The resulting ground clause  $\perp$  is then processed by replacing each term in a + or - placemaker with a variable
- An input variable (+T) must appear as an output variable with the same type in a previous literal and a constant (#T or -#T) is not replaced by a variable.

$\perp = \text{father}(X, Y) \leftarrow$   
 $\text{parent}(X, Y), \text{male}(X), \text{parent}(\text{kathy}, Y), \text{female}(\text{kathy}).$



# SLIPCOVER

- The initial beam associated with predicate  $P/Ar$  will contain the clause with the empty body  $h : 0.5$ . for each bottom clause  $h : - b_1, \dots, b_m$
- In each iteration of the cycle over predicates, it performs a beam search in the space of clauses for the predicate.
- The beam contains couples  $(Cl, Literals)$  where  $Literals = \{b_1, \dots, b_m\}$
- For each clause  $Cl$  of the form  $Head : - Body$ , the refinements are computed by adding a literal from  $Literals$  to the body.



# SLIPCOVER

- The tuple  $(C', \text{Literals}')$  indicates a refined clause  $C'$  together with the new set  $\text{Literals}'$
- EMBLEM is then executed for a theory composed of the single refined clause.
- LL is used as the score of the updated clause  $(C'', \text{Literals}'')$ .
- $(C'', \text{Literals}'')$  is then inserted into a list of promising clauses.
- Two lists are used,  $TC$  for target predicates and  $BC$  for background predicates.
- These lists have a maximum size



- After the clause search phase, SLIPCOVER performs a greedy search in the space of theories:
  - it starts with an empty theory and adds a target clause at a time from the list  $TC$ .
  - After each addition, it runs EMBLEM and computes the LL of the data as the score of the resulting theory.
  - If the score is better than the current best, the clause is kept in the theory, otherwise it is discarded.
- Finally, SLIPCOVER adds all the clauses in  $BC$  to the theory and performs parameter learning on the resulting theory.





## Experiments - Area Under the PR Curve

System	HIV	UW-CSE	Mondial
SLIPCOVER	$0.82 \pm 0.05$	$0.11 \pm 0.08$	$0.86 \pm 0.07$
SLIPCASE	$0.78 \pm 0.05$	$0.03 \pm 0.01$	$0.65 \pm 0.06$
LSM	$0.37 \pm 0.03$	$0.07 \pm 0.02$	-
ALEPH++	-	$0.05 \pm 0.01$	$0.87 \pm 0.07$
RDN-B	$0.28 \pm 0.06$	$0.28 \pm 0.06$	$0.77 \pm 0.07$
MLN-BT	$0.29 \pm 0.04$	$0.18 \pm 0.07$	$0.74 \pm 0.10$
MLN-BC	$0.51 \pm 0.04$	$0.06 \pm 0.01$	$0.59 \pm 0.09$
BUSL	$0.38 \pm 0.03$	$0.01 \pm 0.01$	-



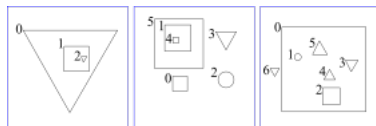
## Experiments - Area Under the PR Curve

System	Carcinogenesis	Mutagenesis	Hepatitis
SLIPCOVER	0.60	$0.95 \pm 0.01$	$0.80 \pm 0.01$
SLIPCASE	0.63	$0.92 \pm 0.08$	$0.71 \pm 0.05$
LSM	-	-	$0.53 \pm 0.04$
ALEPH++	0.74	$0.95 \pm 0.01$	-
RDN-B	0.55	$0.97 \pm 0.03$	$0.88 \pm 0.01$
MLN-BT	0.50	$0.92 \pm 0.09$	$0.78 \pm 0.02$
MLN-BC	0.62	$0.69 \pm 0.20$	$0.79 \pm 0.02$
BUSL	-	-	$0.51 \pm 0.03$



# Bongard Problems

- Introduced by the Russian scientist M. Bongard
- Pictures, some positive and some negative
- Problem: discriminate between the two classes.
- The pictures contain shapes with different properties, such as small, large, pointing down, ... and different relationships between them, such as inside, above, ...



# Input File

<http://cplint.eu/e/bongard.pl>

```
:- use_module(library(slipcover)).  
:- if(current_predicate(use_rendering/1)).  
:- use_rendering(c3).  
:- use_rendering(lpad).  
:- endif.  
:-sc.  
:- set_sc(megaex_bottom, 20).  
:- set_sc(max_iter, 3).  
:- set_sc(max_iter_structure, 10).  
:- set_sc(maxdepth_var, 4).  
:- set_sc(verbosity, 1).
```

See <http://cplint.eu/help/help-cplint.html> for a list of options



## Theory for parameter learning and background

```
bg([]).  
in([  
  (pos:0.5 :-  
    circle(A),  
    in(B,A)),  
  (pos:0.5 :-  
    circle(A),  
    triangle(B))]).
```



# Input File

## Data: two formats, models

```
begin(model(2)).  
pos.  
triangle(o5).  
config(o5,up).  
square(o4).  
in(o4,o5).  
circle(o3).  
triangle(o2).  
config(o2,up).  
in(o2,o3).  
triangle(o1).  
config(o1,up).  
end(model(2)).
```

```
begin(model(3)).  
neg(pos).  
circle(o4).  
circle(o3).  
in(o3,o4).  
.....
```



# Input File

Data: two formats, keys (internal representation)

```
pos(2).  
triangle(2,o5).  
config(2,o5,up).  
square(2,o4).  
in(2,o4,o5).  
circle(2,o3).  
triangle(2,o2).  
config(2,o2,up).  
in(2,o2,o3).  
triangle(2,o1).  
config(2,o1,up).
```

```
neg(pos(3)).  
circle(3,o4).  
circle(3,o3).  
in(3,o3,o4).  
square(3,o2).  
circle(3,o1).  
in(3,o1,o2).  
.....
```



# Input File

- Folds
- Target predicates: `output (<predicate>)`
- Input predicates are those whose atoms you are not interested in predicting

```
input_cw (<predicate>/<arity>).
```

True atoms are those in the interpretations and those derivable from them using the background knowledge

- Open world input predicates are declared with

```
input (<predicate>/<arity>).
```

the facts in the interpretations, the background clauses and the clauses of the input program are used to derive atoms





# Input File

```
fold(train, [2, 3, 5, ...]).  
fold(test, [490, 491, 494, ...]).  
output (pos/0).  
input_cw(triangle/1).  
input_cw(square/1).  
input_cw(circle/1).  
input_cw(in/2).  
input_cw(config/2).
```



# Input File

- Language bias
- *determination*( $p/n, q/m$ ): atoms for  $q/m$  can appear in the body of rules for  $p/n$

```
determination(pos/0, triangle/1).
determination(pos/0, square/1).
determination(pos/0, circle/1).
determination(pos/0, in/2).
determination(pos/0, config/2).
modeh(*, pos).
modeb(*, triangle(-obj)).
modeb(*, square(-obj)).
modeb(*, circle(-obj)).
modeb(*, in(+obj, -obj)).
modeb(*, in(-obj, +obj)).
modeb(*, config(+obj, -#dir)).
```



## Search bias

```
lookahead(logp(B), [(B=_C)]).
```



# Bongard Problems

- Parameter learning

```
induce_par([train], P),  
  test(P, [test], LL, AUCROC, ROC, AUCPR, PR) .
```

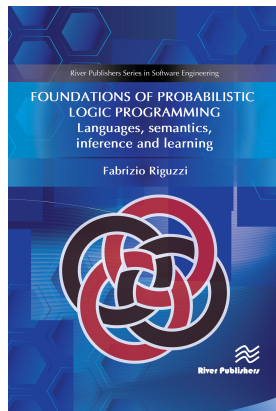
- Structure learning

```
induce([train], P),  
  test(P, [test], LL, AUCROC, ROC, AUCPR, PR) .
```



# Conclusions

- Exact inference
- Approximate inference
- Parameter learning
- Structure learning
- Research directions:
  - Structure learning search strategies
  - Learning hybrid programs
  - Learning restricted and cheaper languages



# Resources

- **Online course on cplint**
  - **Moodle** <https://edu.swi-prolog.org/>
  - **Videos of lectures** <https://www.youtube.com/playlist?list=PLJPXEH0boeND0UGWJxBRWs7qzzKpC-FkN>
- **ACAI summer school on Statistical Relational AI**  
<http://acai2018.unife.it/>
- **Videos of lectures** <https://www.youtube.com/playlist?list=PLJPXEH0boeNDWTNwWTWnVffXi5XwAj1mb>
- **Videos of lecture Probabilistic Inductive Logic Programming**
  - **Part 1** <https://youtu.be/mLdPGSlgNxU>
  - **Part 2** [https://youtu.be/DRlOft0Y\\_Ng](https://youtu.be/DRlOft0Y_Ng)
- **cplint in Playing with Prolog** [https://www.youtube.com/playlist?list=PLJPXEH0boeNAik6QnfvG1AGRQxFY\\_LCE3](https://www.youtube.com/playlist?list=PLJPXEH0boeNAik6QnfvG1AGRQxFY_LCE3)





**THANKS FOR  
LISTENING  
AND  
ANY  
QUESTIONS ?**



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